

CONTENT

Chapter 4: Fundamentals of Image Processing

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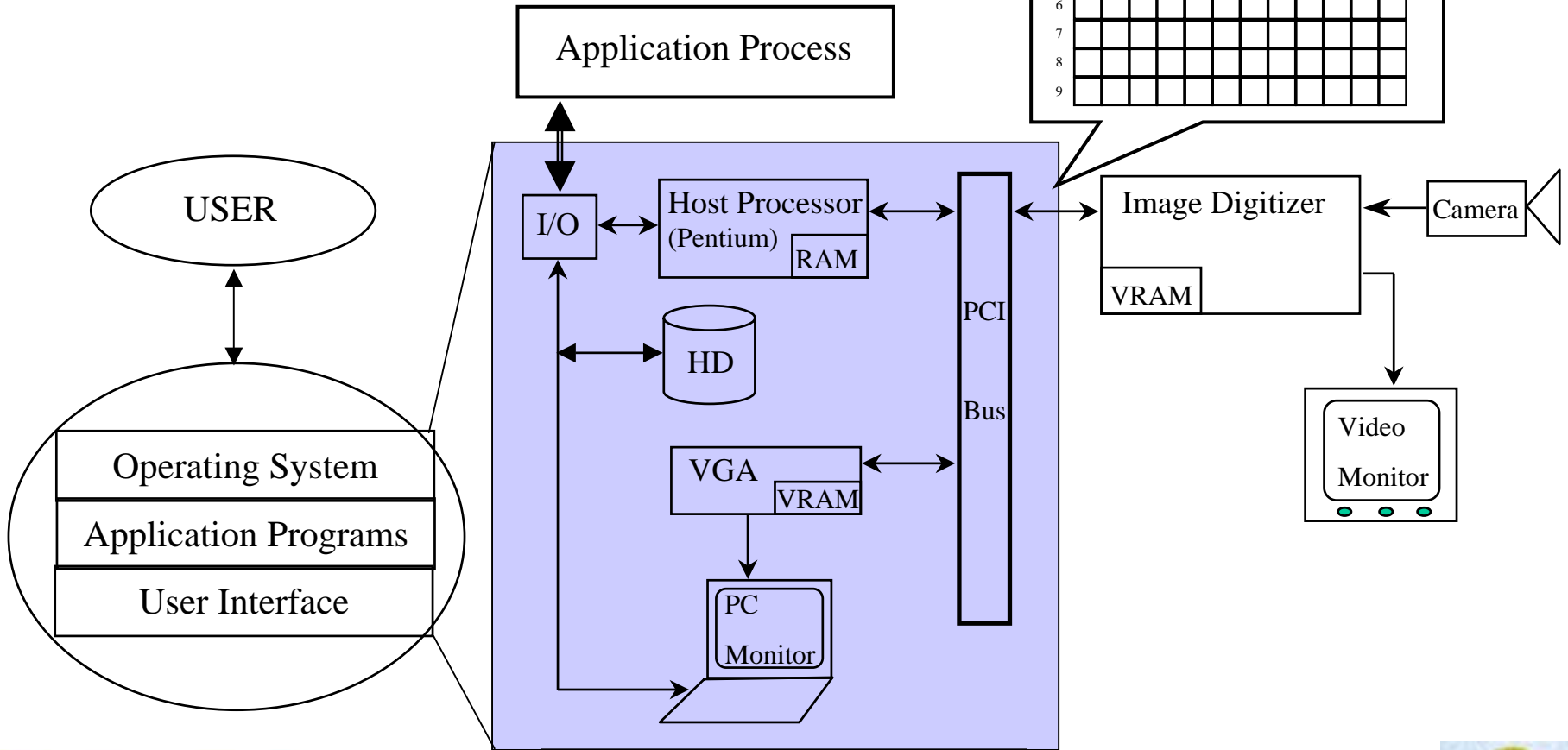
Have Learnt

To Learn



What is a machine vision system ? (A Review)

ANSWER:

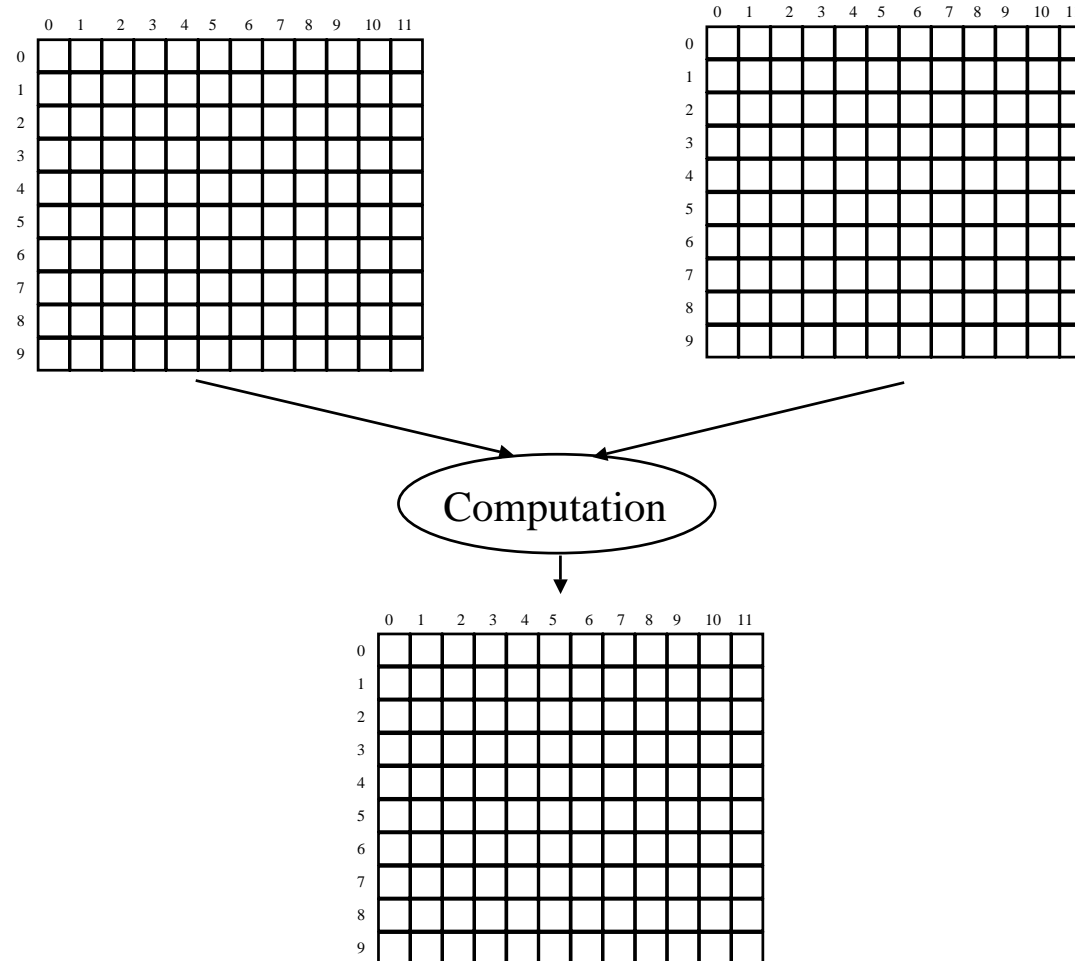


How to do image processing ?



What is a Frame-based image processing technique ?

ANSWER: It refers to the computations carried out on at least two images of the same size.



Frame-based Image Processing Techniques

1. Image Addition:

Input images : $I^{in1} = \{g_{i,j}^{in1} \mid 0 \leq i < n, 0 \leq j < m\}$

$I^{in2} = \{g_{i,j}^{in2} \mid 0 \leq i < n, 0 \leq j < m\}$

Output image : $I^{out} = \{g_{i,j}^{out} \mid 0 \leq i < n, 0 \leq j < m\}$

Operation :

$$g_{i,j}^{out} = a \cdot g_{i,j}^{in1} + (1-a) \cdot g_{i,j}^{in2}.$$

When $a = 0.5$, this computes the average of the two images.



```
#include <stdio.h>

unsigned char image_in1[512*512], image_in2[512*512] ;
unsigned char image_out[512*512] ;

static void ReadInImage()
{
}

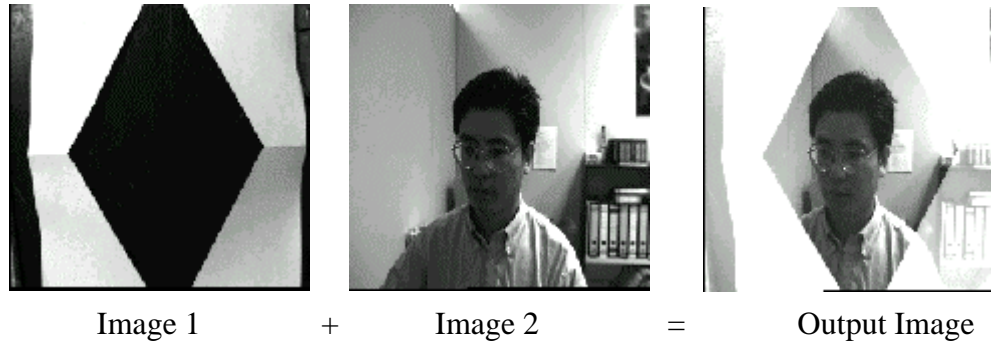
main(int argc, char **argv)
{
    int row, column, a ;

    a = 0.5 ;
    ReadInImage() ;

    for (row = 0; row < 512; row++)
    {
        for (column = 0 ; column < 512; column++)
            image_out[row*512+column] = (unsigned char)
                (a*image_in1[row*512+column] +
                 (1-a)*image_in2[row*512+column]) ;
    }
}
```



Example



Frame-based Image Processing Techniques

2. Image Subtraction:

Input images: $I^{in1} = \{g_{i,j}^{in1} \mid 0 \leq i < n, 0 \leq j < m\}$

$I^{in2} = \{g_{i,j}^{in2} \mid 0 \leq i < n, 0 \leq j < m\}$

Output image: $I^{out} = \{g_{i,j}^{out} \mid 0 \leq i < n, 0 \leq j < m\}$

Operation :

$$g_{i,j}^{out} = |g_{i,j}^{in1} - g_{i,j}^{in2}|.$$




```
#include <stdio.h>

unsigned char image_in1[512*512], image_in2[512*512] ;
unsigned char image_out[512*512] ;

static void ReadInImage()
{
}

main(int argc, char **argv)
{
    int row, column, a ;

    a = 0.5 ;
    ReadInImage() ;

    for (row = 0; row < 512; row++)
    {
        for (column = 0 ; column < 512; column++)
            image_out[row*512+column] = (unsigned char)
                abs(image_in1[row*512+column] -
                    image_in2[row*512+column]) ;
    }
}
```



Example



Image at t1

-



Image at t2

=



Output Image



Example

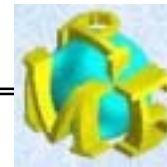
	0	1	2	3	4	5	6	7	8	9	10	11
0	30	30	30	30	30	30	30	30	30	30	30	30
1	30	30	30	30	30	30	30	30	30	30	30	30
2	30	30	66	66	66	66	66	66	66	66	30	30
3	30	30	66	66	66	66	66	66	66	66	30	30
4	30	30	66	66	66	66	66	66	66	66	30	30
5	30	30	30	30	99	99	99	99	30	30	30	30
6	30	30	30	30	99	99	99	99	30	30	30	30
7	30	30	30	30	99	99	99	99	30	30	30	30
8	30	30	30	30	99	99	99	99	30	30	30	30
9	30	30	30	30	30	30	30	30	30	30	30	30

-

	0	1	2	3	4	5	6	7	8	9	10	11
0	30	30	30	30	30	30	30	30	30	30	30	30
1	30	30	30	30	30	30	30	30	30	30	30	30
2	30	30	30	66	66	66	66	66	66	66	66	30
3	30	30	30	66	66	66	66	66	66	66	66	30
4	30	30	30	66	66	66	66	66	66	66	66	30
5	30	30	30	30	30	99	99	99	99	30	30	30
6	30	30	30	30	30	99	99	99	99	30	30	30
7	30	30	30	30	30	99	99	99	99	30	30	30
8	30	30	30	30	30	99	99	99	99	30	30	30
9	30	30	30	30	30	30	30	30	30	30	30	30

=

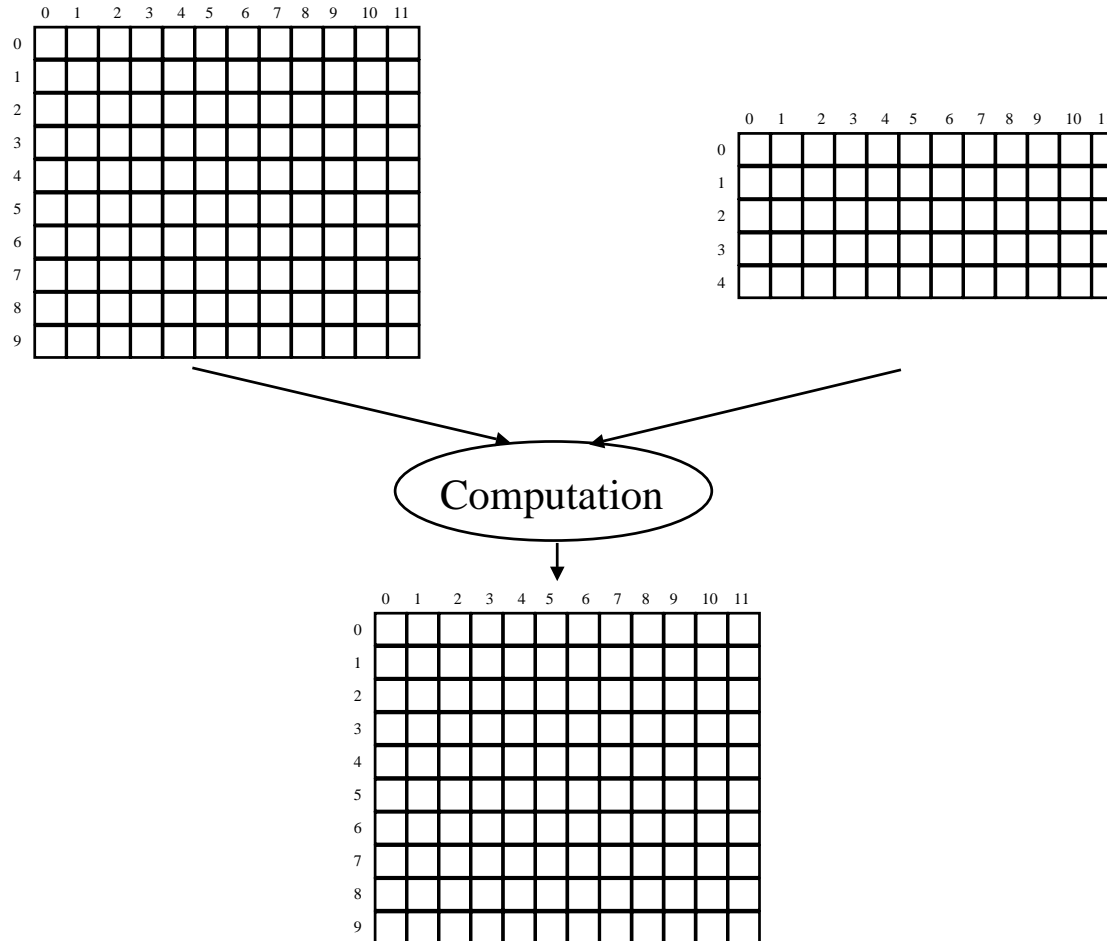
	0	1	2	3	4	5	6	7	8	9	10	11
0	0	0	0	0	0	0	0	0	0	0	0	0
1	0	0	0	0	0	0	0	0	0	0	0	0
2	0	0	36	0	0	0	0	0	0	0	36	0
3	0	0	36	0	0	0	0	0	0	0	36	0
4	0	0	36	0	0	0	0	0	0	0	36	0
5	0	0	0	0	69	0	0	0	69	0	0	0
6	0	0	0	0	69	0	0	0	69	0	0	0
7	0	0	0	0	69	0	0	0	69	0	0	0
8	0	0	0	0	69	0	0	0	69	0	0	0
9	0	0	0	0	0	0	0	0	0	0	0	0



What is a Area-based image processing technique ?

ANSWER:

It refers to the computations carried out on at least two images of different sizes.



Area-based Image Processing Techniques

1. Convolution:

Input images : $I^{in1} = \{g_{i,j}^{in1} \mid 0 \leq i < n, 0 \leq j < m\}$

$I^{in2} = \{g_{i,j}^{in2} \mid 0 \leq i < n_1, 0 \leq j < m_1\}$

Condition : $n_1 < n$ and $m_1 < m$.

Output image : $I^{out} = I^{in1} \otimes I^{in2} = \{g_{i,j}^{out} \mid 0 \leq i < n, 0 \leq j < m\}$

Operation :

$$\left\{ \begin{array}{l} Sub(I^{in1}, i, j) = \{(g_{s,t}^{sub} = g_{i-n_1/2+s, j-m_1/2+t}^{in1}) \mid 0 \leq s < n_1, 0 \leq t < m_1\} \\ g_{i,j}^{out} = \sum_{s=0}^{n_1} \sum_{t=0}^{m_1} (g_{s,t}^{sub} \bullet g_{s,t}^{in2}). \end{array} \right.$$

	0	1	2	3	4	5	6	7	8	9	10	11
0	30	30	30	30	30	30	30	30	30	30	30	30
1	30	30	30	30	30	30	30	30	30	30	30	30
2	30	30	66	66	66	66	66	66	66	66	30	30
3	30	30	66	66	66	66	66	66	66	66	30	30
4	30	30	66	66	66	66	66	66	66	66	30	30
5	30	30	30	30	99	99	99	99	30	30	30	30
6	30	30	30	30	99	99	99	99	30	30	30	30
7	30	30	30	30	99	99	99	99	30	30	30	30
8	30	30	30	30	99	99	99	99	30	30	30	30
9	30	30	30	30	30	30	30	30	30	30	30	30



Illustration

	0	1	2	3	4	5	6	7	8	9	10	11
0	30	30	30	30	30	30	30	30	30	30	30	30
1	30	30	30	30	30	30	30	30	30	30	30	30
2	30	30	66	66	66	66	66	66	66	66	30	30
3	30	30	66	66	66	66	66	66	66	66	30	30
4	30	30	66	66	66	66	66	66	66	66	30	30
5	30	30	30	30	99	99	99	99	30	30	30	30
6	30	30	30	30	99	99	99	99	30	30	30	30
7	30	30	30	30	99	99	99	99	30	30	30	30
8	30	30	30	30	99	99	99	99	30	30	30	30
9	30	30	30	30	30	30	30	30	30	30	30	30

*

-1	0	+1
-1	0	+1
-1	0	+1

What's the pixel value at the location (4,2) of the output image ?



Step 1: At the location (4, 2), get the subimage:

30	66	66
30	66	66
30	30	30

Step 2: Compute the convolution between the sub-image and Image 2:

$$\begin{array}{|c|c|c|} \hline 30 & 66 & 66 \\ \hline 30 & 66 & 66 \\ \hline 30 & 30 & 30 \\ \hline \end{array} * \begin{array}{|c|c|c|} \hline -1 & 0 & +1 \\ \hline -1 & 0 & +1 \\ \hline -1 & 0 & +1 \\ \hline \end{array} = \begin{array}{|c|c|c|} \hline -30 & 0 & 66 \\ \hline -30 & 0 & 66 \\ \hline -30 & 0 & 30 \\ \hline \end{array}$$

Step 3: Compute the sum of the pixel value in the resulting matrix . This sum is the pixel value of the output image at the pixel location (4,2):

$$\text{sum} = 72$$

Output Image

	0	1	2	3	4	5	6	7	8	9	10	11
0												
1												
2												
3												
4			72									
5												
6												
7												
8												
9												



Sample Program

```

unsigned char image1[512*512];
unsigned char image2[3*3];
unsigned char image_out[512*512];

static void DoConvolution()
{
    int i, j, s, t;

    for (i = 3/2; i < 512-3/2; i++)
    {
        for (j = 3/2; j < 512-3/2; j++)
        {
            image_out[i*512+j] = 0;
            for (s = 0; s < 3; s++)
            {
                for (t = 0; t < 3; t++)
                {
                    image_out[i*512+j] = image_out[i*512+j] +
                        (image1[(i-3/2+s)*512+j-3/2+t] * image2[s*3+t]);
                }
            }
        }
    }
}

```

	0	1	2	3	4	5	6	7	8	9	10	11
0	30	30	30	30	30	30	30	30	30	30	30	30
1	30	30	30	30	30	30	30	30	30	30	30	30
2	30	30	66	66	66	66	66	66	66	66	30	30
3	30	30	66	66	66	66	66	66	66	66	30	30
4	30	30	66	66	66	66	66	66	66	66	30	30
5	30	30	30	30	99	99	99	99	30	30	30	30
6	30	30	30	30	99	99	99	99	30	30	30	30
7	30	30	30	30	99	99	99	99	30	30	30	30
8	30	30	30	30	99	99	99	99	30	30	30	30
9	30	30	30	30	30	30	30	30	30	30	30	30



Area-based Image Processing Techniques

2. Template (or Pattern) Matching:

Input images : $I^{in1} = \{g_{i,j}^{in1} \mid 0 \leq i < n, 0 \leq j < m\}$

$I^{in2} = \{g_{i,j}^{in2} \mid 0 \leq i < n_1, 0 \leq j < m_1\}$

Condition : $n_1 < n$ and $m_1 < m$.

Output image : $I^{out} = I^{in1} \oplus (-I^{in2}) = \{g_{i,j}^{out} \mid 0 \leq i < n, 0 \leq j < m\}$

	0	1	2	3	4	5	6	7	8	9	10	11
0	30	30	30	30	30	30	30	30	30	30	30	30
1	30	30	30	30	30	30	30	30	30	30	30	30
2	30	30	66	66	66	66	66	66	66	66	30	30
3	30	30	66	66	66	66	66	66	66	66	30	30
4	30	30	66	66	66	66	66	66	66	66	30	30
5	30	30	30	30	99	99	99	99	30	30	30	30
6	30	30	30	30	99	99	99	99	30	30	30	30
7	30	30	30	30	99	99	99	99	30	30	30	30
8	30	30	30	30	99	99	99	99	30	30	30	30
9	30	30	30	30	30	30	30	30	30	30	30	30

Operation :

$$\left\{ \begin{array}{l} Sub(I^{in1}, i, j) = \{g_{s,t}^{sub} = g_{i-n_1/2+s, j-m_1/2+t}^{in1} \mid 0 \leq s < n_1, 0 \leq t < m_1\} \\ g_{i,j}^{out} = \frac{1}{n_1 \cdot m_1} \cdot \sum_{s=0}^{n_1} \sum_{t=0}^{m_1} |g_{s,t}^{sub} - g_{s,t}^{in2}| \end{array} \right.$$



Illustration

	0	1	2	3	4	5	6	7	8	9	10	11
0	30	30	30	30	30	30	30	30	30	30	30	30
1	30	30	30	30	30	30	30	30	30	30	30	30
2	30	30	66	66	66	66	66	66	66	66	30	30
3	30	30	66	66	66	66	66	66	66	66	30	30
4	30	30	66	66	66	66	66	66	66	66	30	30
5	30	30	30	30	99	99	99	99	30	30	30	30
6	30	30	30	30	99	99	99	99	30	30	30	30
7	30	30	30	30	99	99	99	99	30	30	30	30
8	30	30	30	30	99	99	99	99	30	30	30	30
9	30	30	30	30	30	30	30	30	30	30	30	30

-

30	30	30	30	30
30	30	66	66	66
30	30	66	66	66

What's the pixel value at the location (4,2) of the output image ?



Step 1: At the location (4, 2), get the subimage:

30	30	66	66	66
30	30	66	66	66
30	30	30	30	99

Step 2: Compute “Image Subtraction” between the sub-image and Image 2:

30	30	66	66	66
30	30	66	66	66
30	30	30	30	99

 $-$

30	30	30	30	30
30	30	66	66	66
30	30	66	66	66

 $=$

0	0	36	36	36
0	0	0	0	0
0	0	36	36	33

Step 3: Compute the normalised sum of the values in the resulting image. This sum is the pixel value of the output image at the pixel location (4,2):

$$\text{sum} = 213/15=14$$

0	1	2	3	4	5	6	7	8	9	10	11
0											
1											
2											
3											
4		14									
5											
6											
7											
8											
9											



Program

```

unsigned char image1[512*512];
unsigned char image2[30*30];
unsigned char image_out[512*512];

static void ComputeTemplateMatch()
{
    int i, j, s, t, v;
    for (i = 30/2; i < 512-30/2; i++)
    {
        for (j = 30/2; j < 512-30/2; j++)
        {
            v = 0;
            for (s = 0; s < 30; s++)
            {
                for (t = 0; t < 30; t++)
                {
                    v = v +
                        abs(image1[(i-30/2+s)*512+j-30/2+t]-image2[s*30+t]);
                }
            }
            image_out[i*512+j]=(unsigned char) v/(30*30);
        }
    }
}

```

	0	1	2	3	4	5	6	7	8	9	10	11
0	30	30	30	30	30	30	30	30	30	30	30	30
1	30	30	30	30	30	30	30	30	30	30	30	30
2	30	30	66	66	66	66	66	66	66	66	30	30
3	30	30	66	66	66	66	66	66	66	66	30	30
4	30	30	66	66	66	66	66	66	66	66	30	30
5	30	30	30	30	99	99	99	99	30	30	30	30
6	30	30	30	30	99	99	99	99	30	30	30	30
7	30	30	30	30	99	99	99	99	30	30	30	30
8	30	30	30	30	99	99	99	99	30	30	30	30
9	30	30	30	30	30	30	30	30	30	30	30	30



Area-based Image Processing Techniques

3. Filtering Operations:

Input images : $I^{in1} = \{g_{i,j}^{in1} \mid 0 \leq i < n, 0 \leq j < m\}$

$I^{in2} = \{(g_{i,j}^{in2} \in \{0,1\}) \mid 0 \leq i < n_1, 0 \leq j < m_1\}$

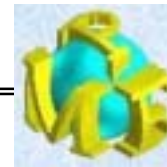
Condition : $n_1 < n$ and $m_1 < m$.

Output image : $I^{out} = \Omega(I^{in1} \otimes I^{in2}) = \{g_{i,j}^{out} \mid 0 \leq i < n, 0 \leq j < m\}$

Operation :

$$\left\{ \begin{array}{l} Sub(I^{in1}, i, j) = \{(g_{s,t}^{sub} = g_{i-n_1/2-s, j-m_1/2-t}^{in1}) \mid 0 \leq s < n_1, 0 \leq t < m_1\} \\ g_{i,j}^{out} = \Omega\{(g_{s,t}^{sub} * g_{s,t}^{in2}) \mid 0 \leq s < n_1, 0 \leq t < m_1\} \\ \Omega = \{\text{Median, Max, Min}\} \end{array} \right.$$

	0	1	2	3	4	5	6	7	8	9	10	11
0	30	30	30	30	30	30	30	30	30	30	30	30
1	30	30	30	30	30	30	30	30	30	30	30	30
2	30	30	66	66	66	66	66	66	66	66	30	30
3	30	30	66	66	66	66	66	66	66	66	30	30
4	30	30	66	66	66	66	66	66	66	66	30	30
5	30	30	30	30	99	99	99	99	30	30	30	30
6	30	30	30	30	99	99	99	99	30	30	30	30
7	30	30	30	30	99	99	99	99	30	30	30	30
8	30	30	30	30	99	99	99	99	30	30	30	30
9	30	30	30	30	30	30	30	30	30	30	30	30



Illustration

Input image

100	102	101	100	99	103
100	102	105	100	102	101
100	102	98	0	101	99
100	25	98	100	102	98
103	100	101	24	102	104
99	101	110	99	103	105
105	101	23	105	10	102
101	100	98	105	102	101

*

1	1	1
1	1	1
1	1	1

0	← min value
98	
98	
100	
100	← median value
101	
102	
102	
105	← max value

Output image

		a			

$$a = \begin{cases} 100. & \text{if } \Omega = \text{Median;} \\ 0. & \text{if } \Omega = \text{Min;} \\ 105. & \text{if } \Omega = \text{Max;} \end{cases}$$



SUMMARY

1. Frame-based processing techniques deal with computations carried out on at least two images of the same size. The common techniques are:
 - * Image addition
 - * Image subtraction
2. Area-based processing techniques deal with computations carried out on at least two images of different sizes. The common techniques are:
 - * Image convolution
 - * Template matching
 - * Filtering operations
(Median, Min, Max)

